

**BROWN UNIVERSITY**  
**PROBLEM SET 10**  
**INSTRUCTOR: SAMUEL S. WATSON**  
**DUE: 1 DECEMBER 2017**

Name:

*Print out these pages, including the additional space at the end, and complete the problems by hand. Then use Gradescope to scan and upload the entire packet by 18:00 on the due date.*

**Problem 1**

Sketch the vector fields  $\mathbf{F}_1(x, y) = \frac{y\mathbf{i} - x\mathbf{j}}{\sqrt{x^2 + y^2}}$  and  $\mathbf{F}_2(x, y) = \frac{y\mathbf{i} - x\mathbf{j}}{x^2 + y^2}$ .

**Solution**

**Problem 2**

Find  $\int_C (x + 2y) dx + x^2 dy$  where  $C$  is the concatenation of the line segment from  $(0, 0)$  to  $(2, 1)$  and the line segment from  $(2, 1)$  to  $(3, 0)$ . (Note: the notation  $(x + 2y) dx + x^2 dy$  is another way of writing  $\mathbf{F} \cdot d\mathbf{r}$ , where  $\mathbf{F} = \langle x + 2y, x^2 \rangle$ .)

**Solution**

Final answer: